



## Cambridge International AS & A Level

CANDIDATE  
NAME

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CENTRE  
NUMBER

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**MATHEMATICS**

**9709/31**

Paper 3 Pure Mathematics 3

**May/June 2021**

**1 hour 50 minutes**

You must answer on the question paper.

You will need: List of formulae (MF19)

### INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

### INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **20** pages. Any blank pages are indicated.







- 4 (a) Prove that  $\frac{1 - \cos 2\theta}{1 + \cos 2\theta} \equiv \tan^2 \theta$ . [2]

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- (b) Hence find the exact value of  $\int_{\frac{1}{6}\pi}^{\frac{1}{3}\pi} \frac{1 - \cos 2\theta}{1 + \cos 2\theta} d\theta$ . [4]

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- 5 (a) Solve the equation  $z^2 - 2piz - q = 0$ , where  $p$  and  $q$  are real constants. [2]

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In an Argand diagram with origin  $O$ , the roots of this equation are represented by the distinct points  $A$  and  $B$ .

- (b) Given that  $A$  and  $B$  lie on the imaginary axis, find a relation between  $p$  and  $q$ . [2]

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(b) Verify by calculation that  $a$  lies between 1.3 and 1.5. [2]

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(c) Use an iterative formula based on the equation in part (a) to determine  $a$  correct to 2 decimal places. Give the result of each iteration to 4 decimal places. [3]

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